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# OPTIMUM ALLOCATION OF A SMALL SCALE CROP FARMLAND IN CHEGUTU OF MASHONALAND WEST PROVINCE, ZIMBABWE

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## ABSTRACT

This paper assesses the economic activity on a small scale farm in which maize, tobacco and vegetables (cabbages, tomatoes and beans) are grown. An operation research model was used to optimize the limited resources available. By comparison with the farmer's farming practices based on intuition and experience the Linear programming method developed showed that the available resources were not optimally allocated. By implementing the linear programming model the optimal crop pattern revealed a rise in the profit margin by 40.3%.

## 1. INTRODUCTION

Optimization using linear programming methods is widely used in agriculture. For instance, in India approximately 70% of the population relies on agriculture for their livelihood (Fazile and Ashraf, 2006; Sofi et al., 2015). To accommodate the ever increasing Indian population its government provided more agricultural land for cultivation. However over the years there has also been a high demand for residential and industrial land which greatly constrained the expansion of agricultural land. In order to efficiently and effectively utilize the available yet limited farming land the agricultural experts had to resort to operation research techniques to resolve the impending food crisis and consequently improve its people's livelihood (Sofi et al, 2015). A similar scenario is observed in Zimbabwe where the majority of the population depends on agriculture for their livelihood (Mugabe, et al 2014). The bulk of the land allocated to new farmers in Zimbabwe are underutilized because of a number of reasons which among them are, the use of traditional farming methods which may not follow the optimal path, insecure land tenure system which incentivize investment, limited access to input and output market, credit and off farm employment (Rukuni, 2006; Mugabe et al., 2014). Linear programming is an effective technique to produce optimal solutions in rural farms in Zimbabwe (Majeke, 2013; Mugabe, 2014). The planning of crop farming entails consideration of resources such as land, accessibility to irrigation water, labour, capital, cropping patterns, cropping intensity, topography and climate (Sarker and Quaddus, 2002; Sofie et al, 2015). Of the several optimization techniques available the Linear Programming model (LP) is the most used because of its proportionate allocation characteristic (Sofie et al, 2015). In the past and even now many small scale farmers rely on intuition and experience to allocate the farm resources available (Kumari et al., 2014, Majeke, 2013). We however want to demonstrate that using the Linear programming models gross income returns are optimal. Nordin Mohamad and Fatimah Said (2011) introduced an LP crop mix model for a finite time planning horizon under limited land and monetary resources to maximize the gross margin at the end of the planning period. An LP problem to determine optimal structure of crops and different method which take into account the income and expenditure of crops per hectare were used for optimizing profit by Ion Raluca, Andreen and Turek Rahdranu Adrian (2012). Majeke (2013) demonstrated how Linear programming (LP) is used to find the optimum combination of crop farm enterprise. His study focused on small scale farmers who often lack operation research techniques to resource allocation problems. Majeke found out that by using the LP technique the gross income rose by 44.65%. A linear programming approach to combination of crop, monogastric farm animals and fish enterprises in Ohafia agricultural zone, Nigeria was studied by Igwe *et al.* (2013) and the optimum gross margin rose by 72.90% compared to the existing plan then. A farm resource allocation problem using LP was also investigated by Kwaku Dei Antwi (2016) who used LP to determine the optimal crop allocation plan for women farmers under land, labor and capital constraints. The LP showed a 13.6% increase in the gross income. Additional literature contributing to the development and use of operation research include (Hossan et al., 2012; Tanko et al., 2011; Day and Mukhopadhyay, 2010; Hossan et al., 2005; Ibrahim et al., 2004; Campbell et al., 1996; Osborn, 1983; Montazemi and Wright, 1982). Using LP model, this study seeks to determine the optimal crop pattern under labor, land and capital constraints allowing the farmer to have optimal profit margin.

## 2. METHODOLOGY

The study was conducted at a farm in Chegutu, located in Mashonaland West province of Zimbabwe. The 5 ha small farm grows maize, tobacco, beans, cabbages and tomatoes as dictated by market forces in the area. Although

the farmer realized profits in his farming activity the rising costs of living in the country has prompted the farmer to find ways of maximizing profits so as to cushion the ever rising cost of living in the country. To eliminate doubt on the applicability of the result generated by the LP model the following assumptions were adopted.

1. The prize of the crop and its yield does not change during the planning period.
2. Availability of farm land, irrigation water, fertilizer, labour, and seed does not change during the planning period.
3. The land is equally suitable for all the selected crops. You can substitute any one crop with another for any hectare piece of land on the farm.

**The linear Programming Model**

The objective function,  $z$  in a Linear Programming Problem (LPP) reads

$$\text{Maximize } z = \sum_{i=1}^n c_i x_j \quad x_j \geq 0, \quad j = 1, 2 \dots, n$$

Subject to the constraints

$$\begin{aligned} a_{11}x_1 + a_{12}x_2 + a_{13}x_3 + \dots + a_{1n}x_n &\leq b_1 \\ a_{21}x_1 + a_{22}x_2 + a_{23}x_3 + \dots + a_{2n}x_n &\leq b_2 \\ a_{31}x_1 + a_{32}x_2 + a_{33}x_3 + \dots + a_{3n}x_n &\leq b_3 \\ &\vdots \\ a_{m1}x_1 + a_{m2}x_2 + a_{m3}x_3 + \dots + a_{mn}x_n &\leq b_m \end{aligned}$$

$$x_i \geq 0, \quad i = 1, 2, \dots, n$$

The Linear Programming Problem (LPP) may be written in a more compact way as,

$$\text{Maximize } z = \sum_{i=1}^n c_i x_j \quad x_j \geq 0, \quad j = 1, 2 \dots, n$$

$$\text{Subject to } \sum_{j=1}^n A_{ij}x_j \leq b_i \quad i = 1, 2, \dots, m; \quad j = 1, 2, \dots, n; \quad x_j \geq 0,$$

where the input variables are represented by  $x_j$ , the cost coefficients of the objective function  $z$  are represented by  $c_i$ , the constraints are bounded above by  $b_i$  and the coefficients of the constraints equations, referred to as the 'production coefficients' are represented by  $a_{ij}$  and the coefficient matrix for the constraints inequalities is given by  $A_{ij}$ .

The farm under study has 5 ha of available farming land. The farmer grows a variety of crops which includes maize, tobacco, cabbages, beans, and tomatoes. The farmer's plan prior using LP technique is depicted in **Table 1**.

**Table 1:** Farmer's plan before optimization for the period 2016-2017

|  | maize | Cabbages | tobacco | beans    | Tomatoes | available |
|--|-------|----------|---------|----------|----------|-----------|
| Land (ha)                              | 2     | 0.5      | 1.4     | 0.6      | 0.3      | 5.0       |
| Gross income (US\$)                    | 7 000 | 4 833.50 | 10 500  | 4 000.20 | 1 500    | 24 334    |
| Labour (US\$)                          | 200   | 206      | 2100    | 240      | 135      | 3 000     |
| Pesticides/fungicides/fertilizer(US\$) | 920   | 450      | 1 428   | 480      | 270      | 4 500     |
| Other operations(\$)                   | 1100  | 1675     | 3472    | 864      | 285      | 9 000     |
| Total expenses(US\$)                   | 2 220 | 2 331    | 7 000   | 584      | 690      | 13 825    |

To determine the production coefficients,  $a_{ij}$ , it is necessary to find the amount of particular input  $x_j$  required to produce 1ha of maize, cabbage, tobacco, beans and tomatoes. A matrix of these coefficients including the expected output per hectare is shown in **Table 2**.

**Table 2:** Farmer's plan per hectare of each crop

|  | maize | cabbages | tobacco | Beans | tomatoes | available    |
|--|-------|----------|---------|-------|----------|--------------|
| land (ha)                              | 1     | 1        | 1       | 1     | 1        | $\leq 5$     |
| Gross income (US\$)                    | 3 500 | 9 667    | 7 500   | 6 667 | 5 000    |              |
| Labour (US\$)                          | 100   | 411      | 1 500   | 400   | 450      | $\leq 3 000$ |
| Pesticides/fungicides/fertilizer(US\$) | 460   | 900      | 1 020   | 800   | 900      | $\leq 4 500$ |
| Other operations(US\$)                 | 550   | 3350     | 2480    | 1440  | 950      | $\leq 9 000$ |

Intuition and farming experience over the years 2014 – 2016 has prompted the farmer to allocate the 5 hectares of land as follows: 2 ha for maize production, 0.5 ha for cabbage production, 1.4 ha for growing tobacco, 0.6 ha for beans production and 0.3 ha for growing tomatoes. Prior LP, the farmer's expected income was US\$7 000 from 2ha of maize, US\$4 833 from 0.5 ha of cabbage, US\$10 500 from 1.4 ha of tobacco, US\$4 000 from 0.6 ha of beans and US\$1 5 00 from 0.3ha of tomatoes. The farmer realized a gross income of US\$ 27 833.70. The size of land allocated for maize and tomatoes were determined by the immediate neighborhood demand and so the farmer had to grow at least 1 ha of maize and 0.2 ha of tomatoes.

In order to apply the LP technique the farmer had to decide on the size of land allocated to each crop. The decision or input variables are:

- $x_1$  = hectares of land allocated for maize production
- $x_2$  = hectares of land allocated for cabbage production
- $x_3$  = hectares of land allocated for tobacco production
- $x_4$  = hectares of land allocated for beans production
- $x_5$  = hectares of land allocated for tomatoes production

The farmer's objective is to maximize total gross margin of producing the crops less costs of transport, fertilizer, pesticides, fungicides, insecticides, seed, irrigation, labour and other operational costs such as electricity, insurance and marketing. The LP model is derived from **Table 2** which depicts the farmer's gross income, expenses and limitations per hectare of each crop type. The LP model is given by

$$\text{Max } z = 3\,500x_1 + 9\,667x_2 + 7\,500x_3 + 6\,667x_4 + 5\,000x_5 \text{ (Objective function)}$$

Subject to,

$$x_1 + x_2 + x_3 + x_4 + x_5 \leq 5 \text{ (Land constraint)}$$

$$1\,00x_1 + 411x_2 + 1\,500x_3 + 4\,00x_4 + 450x_5 \leq 3\,000 \text{ (labour constraint)}$$

$$460x_1 + 900x_2 + 1\,020x_3 + 800x_4 + 900x_5 \leq 4\,500 \text{ (pesticides/fungicides\& fertilizer constraint)}$$

$$550x_1 + 3350x_2 + 2480x_3 + 1\,440x_4 + 950x_5 \leq 9\,000 \text{ (other operations)}$$

$$x_1 \geq 1.0 \text{ (maize land constraint)}$$

$$x_4 \geq 0.2 \text{ (tomatoes land constraint)}$$

$$x_1, x_2, x_3, x_4, x_5, x_6 \geq 0 \text{ (non-negativity constraint)}$$

### 3. RESULTS AND DISCUSSIONS

The crop planning scheme was formulated as a Linear Programming Problem and solved using simplex method using a software package found in Microsoft excel 2017. The farmer's plan without optimization is depicted in **Table 1**. The expenditure, gross income and profit realized by the farmer using the traditional approach are shown in **Table 3**.

**Table 3: Expenditure, gross income and profit before optimization**

|                          | Maize | cabbages | tobacco | Beans    | Tomatoes | Total            |
|--------------------------|-------|----------|---------|----------|----------|------------------|
| land (ha)                | 2     | 0.5      | 1.4     | 0.6      | 0.3      | 5                |
| Gross income (US\$)      | 7000  | 4 833.50 | 10 500  | 4 000.20 | 1 5 00   | <b>27 833.70</b> |
| Expenditure (US\$)       | 2220  | 2331     | 7000    | 1 584    | 690      | <b>13 825</b>    |
| Net income/Profit (US\$) |       |          |         |          |          | <b>14 008.70</b> |

Using intuition and experience (traditional approach) the farmer was realizing a net profit of US\$14 008.70. **Table 4** shows the crop planning scheme as suggested by the LP model. The LP approach suggests that the farmer should grow 1ha of maize, 1.46ha of cabbages, 2.34 ha of beans, 0.2 ha of tomatoes and reserve no piece of land for tobacco.

**Table 4: Optimum farming pattern using LP approach**

|                             | Maize | cabbage   | beans     | tomatoes | total            |
|-----------------------------|-------|-----------|-----------|----------|------------------|
| land (ha)                   | 1     | 1.46      | 2.34      | 0.2      | 5                |
| Labour (US\$)               | 100   | 600.06    | 936       | 90       | 1726.06          |
| pesticides/fertilizer(US\$) | 460   | 1 314     | 1872      | 180      | 3826             |
| Other operations(US\$)      | 550   | 4891      | 3369.60   | 190      | 9000             |
| Expenditure (US\$)          | 1110  | 6805.06   | 6177.60   | 460      | <b>14 552.66</b> |
| gross income (US\$)         | 3500  | 14 113.82 | 15 600.78 | 1 000    | <b>34 214.6</b>  |
| Profit (US\$)               | 2390  | 7 308.76  | 9423.18   | 540      | <b>19 661.94</b> |

**Table 5** depicts the proportion of land allocated for each of the crops in both the existing and optimal plan.

| Cropping pattern    | Existing Plan (ha) |     | Optimal plan (ha) |      |
|---------------------|--------------------|-----|-------------------|------|
|                     | Size of farm       | %   | size of farm      | %    |
| 1. maize            | 2                  | 40  | 1                 | 20   |
| 2. cabbages         | 0.5                | 10  | 1.46              | 29.2 |
| 3. tobacco          | 1.4                | 28  | 0                 | 0    |
| 4. beans            | 0.6                | 12  | 2.34              | 46.8 |
| 5. Tomatoes         | 0.3                | 6   | 0.2               | 4    |
| 6. unused farm land | 0.2                | 4   | 0                 | 0    |
| Total               | 5                  | 100 | 5                 | 100  |

It is deduced from **Table 5** that the farmer was using **96%** of the available farm land in the existing plan whereas in the optimal plan (LP model) the farmer should use all of the available land (**100%**). In the optimal plan **20%** of the available plan is reserved for growing maize compared to **40%** in the existing plan. Although maize is a staple food in Zimbabwe whose demand can never be exhausted the LP technique suggests that growing cabbages and beans is more profitable.

Information displayed in **Table 5** and depicted more clearly in **Figure 1** shows the proportion (expressed as a percentage) of land allocated for each of the crops in both the farmers plan and the LP optimal plan.

**Figure 1:** Bar chart depicting the percentage of land allocated for each of the crops in both the existing and optimal plan

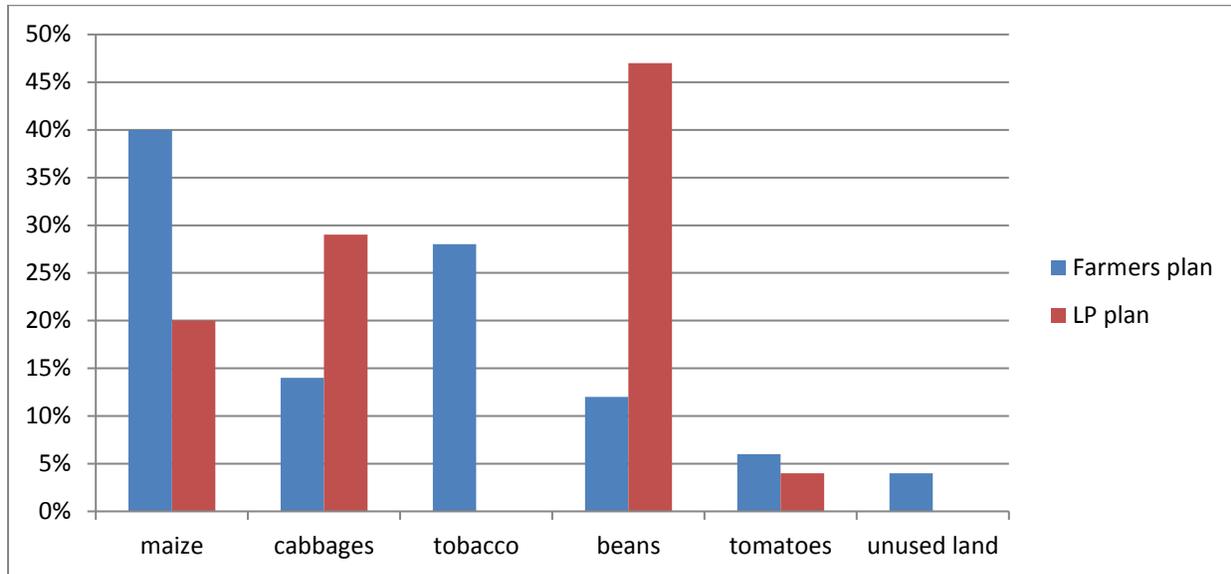


Table 6 gives a comparison of the gross income, expenditure and profit of the traditional and LP approaches.

**Table 6: Comparison of the Gross income, expenditure and net income of the traditional and LP approaches**

|                      | Gross income(US\$) | Expenditure( US\$) | Net income/profit (US\$) |
|----------------------|--------------------|--------------------|--------------------------|
| Traditional approach | 27 833.70          | 13 825.00          | 14 008.70                |
| LP approach          | 34 213.66          | 14 552.66          | 19 661.00                |

Using LP technique the gross income is **US\$34 213.66** compared to **US\$27 833.70** realized from the traditional approach. Less expenses the LP technique has increased the profit margin by **40.3%**. Without maize and tomatoes land constraint the LP technique suggests growing **0.94** ha of cabbage, **4.06** ha of beans and none of tobacco, maize and tomatoes. The gross income would be **US\$ 36 162.23** which raises the profit margin to **50.4%**. The last option is unlikely because in as much as the farmer would like to make profit, he also has to meet the demands of his immediate neighborhood for provision of their staple food as a way of appreciating the community in which the business is based.

#### 4. CONCLUSION

The objective of this study was to implement the Linear programming model to the optimal allocation of farm resources which are subjected to labor, land and capital constraints so as to maximize the profit margin by a small scale farmer in Chegutu which is located in Mashonaland West province of Zimbabwe.

The study revealed that the existing farming plan which is based on intuition and experience has resulted in suboptimal allocation of available resources although the farmer was making some profit. A comparative analysis of results obtained using the LP model and the existing farming method showed that the LP model increased the profit margin by **40.3 %**, by growing maize, cabbages, tomatoes, beans and no tobacco. The results of the study suggest the use of the LP model for optimal profit margins.

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